Journal of Modern Applied Statistical Methods

Volume 14 | Issue 1

Article 14

5-1-2015

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Recommended Citation

Cangur, Sengul and Ercan, Ilker (2015) "Comparison of Model Fit Indices Used in Structural Equation Modeling Under Multivariate Normality," *Journal of Modern Applied Statistical Methods*: Vol. 14 : Iss. 1, Article 14. DOI: 10.22237/jmasm/1430453580

Comparison of Model Fit Indices Used in Structural Equation Modeling Under Multivariate Normality

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The purpose of this study is to investigate the impact of estimation techniques and sample sizes on model fit indices in structural equation models constructed according to the number of exogenous latent variables under multivariate normality. The performances of fit indices are compared by considering effects of related factors. The Ratio Chi-square Test Statistic to Degree of Freedom, Root Mean Square Error of Approximation, and Comparative Fit Index are the least affected indices by estimation technique and sample size under multivariate normality, especially with large sample size.

Keywords: Structural equation modeling, multivariate normality

Introduction

Modeling methods are employed for studying the phenomena than require the utilization of complex variable set. Structural Equation Modeling (SEM) is preferred when studying the causal relations and the latent constructs among the variables is in question. The reason is it can be used to analyze complex theoretical models and its practicability.

The objective of SEM is to explain the system of correlative dependent relations between one or more manifest variables and latent constructs simultaneously. It serves to determine how the theoretical model that denotes relevant systems is supported by sample data, i.e., estimation of relations between the main constructs. Because there is no single criterion for the theoretical model fit evaluation obtained as a result of SEM, a wide array of fit indices was developed (Schermelleh-Engel and Moosbrugger, 2003; Ding et al., 1995; Sugawara and MacCallum, 1993). Studies conducted through SEM were

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undertaken by using empirical and non-empirical data so as to develop and confirm theory (Bentler and Dudgeon, 1996; Wang et al., 1996; Bentler, 1994).

Simulation studies were conducted to test the robustness of SEM, because the assumptions required usually cannot be verified in practice. Because these studies were conducted in order to verify hypothesis, a known theoretical model was taken as a reference and the behaviors of the most commonly used techniques in specific conditions were observed. The parameter estimations obtained through the estimation techniques based on various distributional conditions and sample size, standard errors and the bias of model fit indices were researched in the studies conducted.

Studies were conducted for recommending and improving the parameter estimation techniques used in SEM and selecting the conditions in which these are to be used (Boomsma and Hoogland, 2001; Wang et al., 1996; Chou and Bentler, 1995; Bentler, 1994). Other studies were conducted by employing various empirical designs so as to examine the effects of factors such as estimation techniques, sample sizes, distributional conditions, number of latent variables, number of manifest variables, the misspecification degree of the model, factor loads, factor correlations, improper solutions, convergence errors on model fit indices make contribution to the SEM literature (e.g., Herzog & Boomsma, 2009; Fan & Sivo, 2007; Sivo et al., 2006; Lei & Lomax, 2005; Marsh et al., 2004; Boomsma and Hoogland, 2001; Fan et al., 1999; Hu & Bentler, 1998, 1999; Wang et al., 1996; Chou and Bentler, 1995; Ding et al., 1995; Marsh & Balla, 1994; Sugawara and MacCallum, 1993; Gerbing & Anderson, 1992).

Hence, a wide array of simulation studies were conducted on model fit indices through various estimation techniques. Unlike these studies, in the current study the inclusion of a higher number of estimation techniques was used. Furthermore, the differentiation of the model structure was agreed to be studied as exogenous factor rather than an effect so as to reach a mutual interpretation. The effects of estimation technique and sample size factors on model fit indices were examined in circumstances in which the multivariate normality assumption was ensured and in the models which were established by taking exogenous (independent) latent variables into consideration in the research. The model fit indices were compared to recommend appropriate model fit indices in line with the effects of these factors.

Methodology

Maximum likelihood estimation technique

Maximum likelihood estimation (MLE) technique is one of the normal theory estimation techniques that is able to provide model parameter estimations simultaneously (Kline, 2011; Chou and Bentler, 1995). Assume a $\{\mathbf{x}_1, \mathbf{x}_2, ..., \mathbf{x}_n\}$ random sample is derived from multivariate normal distribution $N(\boldsymbol{\mu}_0, \boldsymbol{\Sigma}_0)$. In order to achieve $\boldsymbol{\Sigma}_0 = \boldsymbol{\Sigma}(\boldsymbol{\theta}_0)$, assumed there is population (true) matrix function with $\boldsymbol{\Sigma}_0, q \times 1$ size and $\boldsymbol{\theta}_0$ unknown parameter. In this case, MLE function can be defined as in equation (1).

$$\mathbf{F}_{\mathrm{MLE}}\left(\mathbf{\theta}\right) = \log\left|\mathbf{\Sigma}\left(\mathbf{\theta}\right)\right| + tr\left(\mathbf{S}\mathbf{\Sigma}\left(\mathbf{\theta}\right)^{-1}\right) - \log\left|\mathbf{S}\right| - p \tag{1}$$

S denotes sample covariance matrix while $\Sigma(\theta_0)$ indicates the covariance matrix of the hypothesized model, *tr* denotes the trace of matrix and *p* represents the number of manifest variables (Lee, 2007).

Generalized least squares technique

The GLS technique makes multivariate normality assumption flexible compared to MLE technique, yet also features the assumptions of MLE technique. GLS function can be given as follows.

$$\mathbf{F}_{\text{GLS}}\left(\boldsymbol{\theta}\right) = 2^{-1} tr\left\{\left(\mathbf{S} - \boldsymbol{\Sigma}\right)\mathbf{V}\right\}^{2}$$
(2)

The population and sample covariance matrices are indicated with Σ and **S** respectively. The **V** matrix can be a constant positive definite matrix or a stochastic matrix which converges to Σ_0^{-1} . The GLS function reduces to the least squares function when **V** equals to identity matrix (**I**) (Lee, 2007).

Asymptotically distribution-free technique

The Asymptotically Distribution-Free (ADF) technique does not require multivariate normality assumption and is based on the calculation of **W** weighted matrix and GLS estimation. Accordingly, assume $\mathbf{x}_1, \mathbf{x}_2, ..., \mathbf{x}_n$ are the independent identically distributed observations of a sample with mean vector μ , covariance matrix $\Sigma_0 = \Sigma(\mathbf{\theta}_0)$ and finite eighth-order moments that is not obliged

to be selected from a multivariate normal distribution. $\tilde{\theta}_A$ ADF estimator of θ_0 will be defined as in equation (3) as the vector which minimizes GLS function:

$$\mathbf{F}_{\mathrm{ADF}}\left(\boldsymbol{\theta}\right) = 2^{-1} \left[\operatorname{vecs}\left\{ \mathbf{S} - \boldsymbol{\Sigma}\left(\boldsymbol{\theta}\right) \right\} \right]^{\prime} \mathbf{W}^{-1} \left[\operatorname{vecs}\left\{ \mathbf{S} - \boldsymbol{\Sigma}\left(\boldsymbol{\theta}\right) \right\} \right]$$
(3)

Here *vecs* denotes the column vector which is obtained through derivation of lower triangle matrix components row by row. W is the stochastic weighted matrix with positive definite and is assumed to converge to Σ^* (Lee, 2007). Many researchers emphasized the requirement to work with large sample sizes so as to ensure that ADF estimations have the desired asymptotical properties (i.e., Bentler & Dudgeon, 1996).

Satorra-Bentler scaled chi square test statistic

The normal theory chi-square statistic can be adjusted for its convergence to the referenced chi-square distribution even if it is not fit for the expected chi-square distribution in circumstances where the normality assumption is violated. Satorra-Bentler scaled χ^2 test statistic can be indicated as follows:

$$\chi_{\rm SB}^2 = \frac{\chi_{\rm MLE}^2}{\varpi} \tag{4}$$

 χ^2_{MLE} denotes the chi-square value of MLE technique. The ϖ constant, also known as the scaling factor, is a function of the model-implied weighted matrix, the multivariate kurtosis index and the degree of freedom for the model (Finney and Distefano, 2006; Chou and Bentler, 1995). Provided that multivariate kurtosis is not in question χ^2_{MLE} value is equal to χ^2_{SB} value, and two chi-square values are obtained as different from each other only on the event of the degree of multivariate kurtosis increases (Finney and Distefano, 2006).

Commonly-used model fit indices in SEM

 χ^2 and χ^2 / v Ratio The χ^2 test statistic is an absolute fit index which assumes multivariate normality and is sensitive to sample size (Gerbing and Anderson, 1992). This test statistic

$$\chi^{2} = -2\left\{-\frac{1}{2}\left(n-1\right)\left[tr\left(\mathbf{S}\boldsymbol{\Sigma}^{-1}\right) + log\left|\boldsymbol{\Sigma}\right| - log\left|\mathbf{S}\right| - p\right]\right\} = (n-1)\mathbf{F}$$
(5)

is distributed the central χ^2 with degree of freedom { $\frac{1}{2}p(p+1)$ } – t in large samples. Here p, denotes the number of observed variables and t symbolizes the number of estimated independent parameters. **S** denotes unrestricted sample covariance matrix whereas $\Sigma(\theta)$ denotes restricted covariance matrix. It is said that the larger the likelihood related to χ^2 , the closer the fit between the hypothesized model and the perfect model (Herzog and Boomsma, 2009; Hu and Bentler, 1995). This statistic is dependent on sample size. With increasing sample size and a fixed number of degree of freedom, the χ^2 value increases. This signs to the problem that plausible models might be rejected (Schermelleh-Engel and Moosbrugger, 2003).

 χ^2/ν , χ^2 is an index obtained by dividing the test statistic value by the degree of freedom (ν). It is known as parsimony and stand-alone fit index. The development of Tucker-Lewis Index is also based on this ratio. The value of this ratio gives information on the fit between data and model. It is said that with smaller index value of χ^2/ν ratio, the consistency will be better. Schermelleh-Engel and Moosbrugger (2003) stated that this ratio indicates good fit when it produces 2 or a smaller value while it indicates an acceptable value when it produces a value of 3. Ding et al. (1995) stated that this ratio should be close to 1 or have a smaller value.

Standardized Root Mean Square Residual (SRMR) Index The Standardized Root Mean Square Residual (SRMR) is an index of the average of standardized residuals between the observed and the hypothesized covariance matrices (Chen, 2007). This absolute fit index can be indicated as follows:

$$SRMR = \sqrt{\frac{\sum_{i=1}^{p} \sum_{j=1}^{i} \left[\left(s_{ij} - \hat{\sigma}_{ij} \right) / \left(s_{ii} s_{jj} \right) \right]^{2}}{p(p+1)/2}}$$
(6)

where s_{ij} indicates a component of **S** sample covariance matrix and $\hat{\sigma}_{ij}$ shows a component of $\Sigma(\hat{\theta})$ hypothesized model whereas *p* is the number of observed variables. SRMR does not give any information about the direction of

discrepancies between **S** and $\Sigma(\hat{\theta})$ (Kline, 2011; Schermelleh-Engel and Moosbrugger, 2003).

Although SRMR indicates the acceptable fit when it produces a value smaller than 0.10, it can be interpreted as the indicator of good fit when it produces a value lower than 0.05 (Kline, 2011; Hu and Bentler, 1999; Schermelleh-Engel and Moosbrugger, 2003; Lacobucci, 2010). One of the reasons of preferring SRMR index in studies is its relative independence from sample size (Chen, 2007).

Root Mean Square Error of Approximation (RMSEA) Index The RMSEA is an index of the difference between the observed covariance matrix per degree of freedom and the hypothesized covariance matrix which denotes the model (Chen, 2007). This absolute fit index is estimated as follows:

$$RMSEA = \sqrt{max} \left\{ \left(\frac{F(\mathbf{S}, \mathbf{\Sigma}(\hat{\mathbf{\theta}}))}{\nu} - \frac{1}{n-1} \right), 0 \right\}$$
(7)

Here $F(\mathbf{S}, \mathbf{\Sigma}(\hat{\mathbf{\theta}}))$ indicates the fit function is minimized whereas *max* points to the maximum value of the values given in brackets. While *l* is the number of known parameters and *t* is the number of independent parameters, v = l - t indicates the value of the degrees of freedom and *n* indicates the sample size (Schermelleh-Engel and Moosbrugger, 2003).

Observe in equation (7) that RMSEA produces a better quality of estimation when the sample size is large compared to smaller sample sizes. When the sample size is large, the term [1/(n-1)] gets closer to zero asymptotically (Rigdon, 1996).

The RMSEA also takes the model complexity into account as it reflects the degree of freedom as well. RMSEA value smaller than 0.05, it can be said to indicate a convergence fit to the analyzed data of the model while it indicates a fit close to good when it produces a value between 0.05 and 0.08. A RMSEA value falling between the range of 0.08–0.10 is stated to indicate a fit which is neither good nor bad. Hu and Bentler (1999) remarked that RMSEA index smaller than 0.06 would be a criterion that will suffice. A few researchers stated that RMSEA is among the fit indexes which are affected the least by sample size (Marsh et al., 2004; Schermelleh-Engel and Moosbrugger, 2003).

COMPARISON OF MODEL FIT INDICES

Tucker-Lewis Index (TLI) The Tucker-Lewis Index (TLI) is an incremental fit index. Non-Normed Fit Index (NNFI) which is also known as TLI was developed against the disadvantage of Normed Fit Index regarding being affected by sample size. TLI is calculated as given below (Schermelleh-Engel and Moosbrugger, 2003; Ding et al., 1995; Gerbing & Anderson, 1992).

$$TLI = \frac{\left(\chi_{i}^{2} / \nu_{i}\right) - \left(\chi_{t}^{2} / \nu_{t}\right)}{\left(\chi_{i}^{2} / \nu_{i}\right) - 1} = \frac{\left(F_{i} / \nu_{i}\right) - \left(F_{t} / \nu_{t}\right)}{\left(F_{i} / \nu_{i}\right) - \left(1 / (n - 1)\right)}$$
(8)

Here χ_i^2 belongs to the independence model whereas χ_t^2 belongs to the target model. v_i and v_t are the number of degrees of freedom for the independence and target models respectively, in relation to the chi-square test statistics. F is the value of appropriate minimum fit function, and *n* indicates sample size.

The bigger TLI value indicated better fit for the model. Although values larger than 0.95 are interpreted as acceptable fit, 0.97 is accepted as the cut-off value in a great deal of researches. Furthermore TLI is not required to be between 0 and 1 as it is non-normed. The key advantage of this fit index is the fact that it is not affected significantly from sample size (Schermelleh-Engel and Moosbrugger, 2003; Ding et al., 1995; Gerbing & Anderson, 1992).

Comparative Fit Index (CFI) The Comparative Fit Index (CFI) is an incremental fit indices. CFI is a corrected version of relative non-centrality index. The extent to which the tested model is superior to the alternative model established with manifest covariance matrix is evaluated (Chen, 2007) and the equation can be given as in (9).

$$CFI = 1 - \frac{max \left[\left(\chi_t^2 - v_t \right), \ 0 \right]}{max \left[\left(\chi_t^2 - v_t \right), \left(\chi_i^2 - v_i \right), \ 0 \right]}$$
(9)

Here *max* indicates the maximum value of the values given in brackets. χ_i^2 and χ_t^2 are test statistics of the independence model and the target model respectively. v_i and v_t are the degrees of freedom of the independence model and the target model in relation to chi-square test statistics respectively (Schermelleh-Engel and Moosbrugger, 2003; Ding et al., 1995; Gerbing & Anderson, 1992).

The CFI produces values between 0–1 and high values are the indicators of good fit. When CFI value is 0.97, it means that the fit in question is better compared to the independence model. An acceptable fit is in question provided that CFI value is larger than 0.95 (Schermelleh-Engel and Moosbrugger, 2003). This index is relatively independent from sample size and yields better performance when studies with small sample size (Chen, 2007; Hu and Bentler, 1998).

Hypothesized models

Two structural equation models (SEMs) with different structures of mean and covariance, and constructed in accordance with exogenous latent variable number were established. Model 1 is the model with two exogenous and one endogenous latent variables with each of the exogenous variable having two indicators (Figure 1). Model 2 is the other model established through the addition of one exogenous variable with two indicators to the structure given in Model 1 (Figure 2).



Figure 1. Structural equation model with three latent variables, with observed variables each (Model 1)



Figure 2. Structural equation model with four latent variables, with observed variables each (Model 2)

Sample generation

The mean vectors and covariance matrices which were used for generating data are given in Table 1 for identification model. Multivariate normal distribution data were generated by taking Model 1 and Model 2 into consideration for the sample sizes determined as 100, 500 and 1000 units. MLE, GLS, ADF and SB₂ χ^2 techniques were applied to the derived data. SEMs which are significant in accordance to the test statistics were included in the study (p > 0.05). χ^2 / v ratio, SRMR, RMSEA, TLI, and CFI model fit indices which were obtained from the significant SEMs were recorded. A total of 1200 significant SEMs were examined in the research. The simulation and all of the remaining statistical analyses were performed in R software through the utilization of *MSBVAR*, *mvShapiroTest*, *QRMlib* and *lavaan* packages.

Model 1		y 1	y 2	X 1	х	2	X 3	X 4
y 1		1.50						
y 2		1.18	1.50					
X 1		0.95	0.90	1.50				
X 2		0.95	0.90	1.20	1.5	0		
X 3		0.95	0.90	0.50	0.5	0	1.50	
X 4		0.95	0.90	0.50	0.5	0	1.30	1.50
µ1 =		(100	100	100	10	0	100	100)
Model 2	y 1	y 2	X 1	X 2	X3	X 4	X 5	X 6
y 1	1.50							
y 2	1.18	1.50						
X 1	0.95	0.90	1.50					
X 2	0.95	0.90	1.20	1.50				
X 3	0.95	0.90	0.50	0.50	1.50			
X 4	0.95	0.90	0.50	0.50	1.30	1.50		
X 5	0.95	0.90	0.50	0.50	0.50	0.50	1.50	
X 6	0.95	0.90	0.50	0.50	0.50	0.50	1.25	1.50
µ2 =	(100	100	100	100	100	100	100	100)

Table 1. Covariance matrices and Mean vectors of Model 1 and Model 2

 μ_1 : Mean vector of Model 1; μ_2 : Mean vector of Model 2

Study design

The study was designed as 4×3 so as to examine the effects of 4 different estimation techniques (MLE, GLS, ADF and SB₂ χ^2) and 3 different sample sizes (100, 500 and 1000) under multivariate normal distribution condition by taking both structural models into consideration.

A rank transform was applied to each index, and then Factorial Analysis of Variance (Factorial ANOVA) was conducted so as to find out the effects of estimation technique and sample size factors on χ^2 / v ratio, SRMR, RMSEA, TLI and CFI model fit indices based on the models established. Tukey's Honestly Significant Difference (Tukey's HSD) was used for the pairwise comparisons of the factors in which statistically significant differences were found.

Results

Out of the simulation results obtained by applying SEM estimation techniques to Model 1 and Model 2 under multivariate normality condition, 3.17%, 8.60% and 7.6% comprise of the convergence error of model, improper solutions, and the simulations excluded from the study (non-significant SEMs) respectively. As well

as the significance of the models included in the study, it was found that fit indices also have good fit and acceptable fit.

The comparative summarized table of model fit indices based on estimation techniques (*p*-values) is given in Table 2. While no significant differentiation was identified in respect to χ^2/ν ratio obtained from Model 1 based on the estimation techniques and RMSEA indices, differentiations were identified in SRMR, TLI and CFI. Although the CFI was the least affected one from the estimation techniques among the model fit indices which were identified to have differentiations, SRMR was the most affected one. No significant differentiation between the normal theory techniques MLE and GLS or between SB₂ χ^2 and each normal theory was found in respect to CFI. However, CFI obtained with ADF technique was identified to be different from those achieved by the other techniques. In terms of TLI, no significant differentiation was determined between MLE and SB₂ χ^2 techniques and, as for SRMR index, between MLE and GLS techniques (Table 2).

When the entirety of the model fit indices were examined based on the estimation techniques in the structure given in Model 2, it was found that χ^2 / v ratio index was different compared to GLS and ADF techniques, yet these produced similar values in all of the remaining techniques. As for the RMSEA and CFI indices, these were identified to show no difference compared to MLE, GLS and SB₂ χ^2 techniques, yet all of the values obtained with ADF were different from those obtained with the other techniques. In respect to TLI, only MLE and SB₂ χ^2 did not show any significant difference in between (Table 2).

	Model 1	Model 2						
Technique	$\gamma^2 / v^{\mathbf{z}_E} SRMR^{\mathbf{z}} RMSFA^{\mathbf{z}_E}$	TI I [#]	CFI [#]	γ^2 / v^{μ}	SRMR	RMSFA [#]	TI I [#]	CFI
MLE-GLS	0.191	<0.001	0.372	0.42	<0.001	0.471	< 0.001	0.72
MLE-ADF	<0.001	< 0.001	< 0.001	0.068	< 0.001	0.022	<0.001	<0.001
$MLE-SB_{\chi^2}$	<0.001	1.000	0.999	1.000	<0.001	0.999	1.000	0.999
GLS-ADF	<0.001	0.002	0.038	<0.001	<0.001	<0.001	<0.001	<0.001
$GLS-SB_{\chi^2}$	<0.001	<0.001	0.457	0.401	<0.001	0.551	<0.001	0.629
$ADF-SB_{\chi^2}$	<0.001	<0.001	<0.001	0.074	<0.001	0.015	<0.001	<0.001

Table 2. The comparative summarized table of model fit indices based on estimation techniques (*p*-values for Tukey's HSD)

MLE: Maximum Likelihood Estimation; GLS: Generalized Least Squares; ADF: Asymptotically Distribution Free; SB_ χ^2 : Satorra-Bentler Scaled Chi-Square; χ^2 / v :(Chi-Square test statistic/degree of freedom) ratio; SRMR: Standardized Root Mean Square Residual; RMSEA: Root Mean Square Error of Approximation; TLI: Tucker – Lewis Index; CFI: Comparative Fit Index; " : Ranked Value; Degree of Freedom of Model 1 (v₁)= 6; Degree of Freedom of Model 2 (v₂)= 14; £: *p*>0.05 value for Factorial ANOVA

	<i>Model 1</i> Fit Indices						<i>Model 2</i> Fit Indices				
Sample Size	χ^2/v^{a}	SRMR [□]	RMSEA ^ª	TLI⁼	CFI⁼	χ^2 / v^{a}	SRMR [∞]	RMSEA [®]	TLI⁼	CFI⁼	
100-500	0.006	<0.001	0.005	<0.001	<0.001	0.005	<0.001	0.217	<0.001	0.004	
100-1000	0.001	<0.001	0.049	<0.001	<0.001	0.024	<0.001	0.003	<0.001	<0.001	
500-1000	0.786	<0.001	0.705	<0.001	0.862	0.863	<0.001	0.236	<0.001	0.126	

Table 3. The comparative summarized table of model fit indices based on sample sizes (*p*-values for Tukey's HSD)

 (χ^2 / v) : (Chi-Square test statistic/degree of freedom) ratio; SRMR: Standardized Root Mean Square Residual; RMSEA: Root Mean Square Error of Approximation; TLI: Tucker – Lewis Index; CFI: Comparative Fit Index; ": Ranked Value; Degree of Freedom of Model 1 (v_1)= 6; Degree of Freedom of Model 2 (v_2)= 14

The summarized comparative table of model fit indices based on sample size (p-values) is given in Table 3. The index values of SRMR and TLI obtained from Model 1 under multivariate normality condition was found to be significantly different according to sample sizes. However, while χ^2/v ratio, RMSEA and CFI obtained with a sample size of 100 units were observed to be significantly different from those obtained with the sample sizes of 500 and 1000 units, no significant differentiation was observed in none of the three indices obtained in sample sizes of 500 and 1000 units. With the increasing sample size, and in particular, when the sample size was above 500 units, it can be said that no significant change is seen in χ^2/v , RMSEA and CFI values. All model fit indices showed significant differences based on sample size. However, while no significant differentiation was identified when they were examined in respect to χ^2/ν ratio, RMSEA and CFI values based on large sample size (n > 500), significant differentiation was determined according to small and large sample sizes (100 and 1000). Additionally, it was found that there is no difference between the values obtained with small sample sizes (100 and 500) in RMSEA.

Discussion

The empirical evaluation of the proposed models is an important aspect of theory development process. It was determined that the χ^2/ν ratio index based on the structures given in Model 1 and Model 2 was not affected from MLE and SB_ χ^2 techniques, and RMSEA and CFI were not affected from MLE, GLS and SB_ χ^2 . TLI was determined to be insensitive to MLE and SB_ χ^2 techniques, yet SRMR index was affected from all estimation techniques. When the compliance of our findings with the literature is evaluated on the basis of models, it is seen that they

are generally in compliance with the results of the studies conducted by Sugawara and MacCallum (1993), Hu and Bentler (1998, 1999), Fan et al. (1999), and Lei and Lomax (2005) yet entirely incompliant with the results produced by Ding et al. (1995).

When both model structures are taken into consideration in multivariate normal distribution condition and in the event of studying with large sample size; χ^2 / v rate, RMSEA and CFI were determined to be independent from sample size while SRMR and TLI were dependent. When the compliance of our findings with the literature is examined on the basis of models, it was generally in parallel to the study results produced by Lacobucci (2010), Herzog et al. (2009), Jackson, (2001, 2007), Beauducel and Wittmann (2005), Curran et al. (2003), Kenny and McCoach (2003), Curran et al. (2002), Hu and Bentler (1999), Fan et al. (1999), Ding et al. (1995), Marsh and Balla (1994). Yet our findings except *RMSEA* were quite different from the study results of Fan and Sivo (2007). Furthermore, Rigdon (1996) emphasized the requirement to prefer RMSEA with large sample sizes and researches conducted to develop theory in his study in which RMSEA and CFI were compared.

The difference of model structure was accepted as an exogenous factor rather than a primary effect. Therefore, it can be stated that particular model fit indices obtained with only ADF technique are negatively affected from the increase of the number of latent variables when the result is evaluated in respect to the factors examined in this study.

In conclusion, it would be appropriate to prefer χ^2 / v ratio, RMSEA and CFI in the event of studying with large samples and utilization of MLE, GLS and SB_ χ^2 techniques under multivariate normal distribution condition. Furthermore, we do not recommend using SRMR in model fit research as it is the most affected index from estimation technique and sample size.

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COMPARISON OF MODEL FIT INDICES

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